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## OMAE-FPSO'04-0066

### AN IMPROVED VOLUME-OF-FLUID (IVOF) METHOD FOR WAVE IMPACT TYPE PROBLEMS

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#### ABSTRACT

In this paper, a prediction method for wave impact type problems is presented. The method is based on the Navier-Stokes equations that describe flow of an incompressible, viscous fluid. The free surface is displaced using a Volume-of-Fluid based algorithm combined with a local height function. Results are shown of steep wave simulations where the free surface profile is compared to measurements. Furthermore, results of a simulation of green water on the deck of a moving ship are shown.

#### INTRODUCTION

In the offshore industry, increasing use is made of floating systems like FPSO's for the extraction of oil at large water depth. These systems must face all weather types: even during heavy storms they stay at their position. For the development of such structures, there is a great need for simulation tools that can predict the impact loads of green water or steep waves and give insight in local phenomena. Part of the Joint Industry Project SafeFLOW, initiated in January 2001, is devoted to the further development and improvement of a method that is able to predict these local wave impact problems.

The development of the method, called COMFLOW, has started in 1995 with the simulation of liquid-filled spacecraft that are tumbling in space (Gerrits, 2001) and (Gerrits, 2003). In this application in a low-gravity environment, a good numerical han-

dling of the free surface is crucial. Another application has been found in medical science where blood flow through arteries has been studied (Loots, 2003). In 1999 a pilot study of the simulation of green water on the deck of a fixed FPSO has been performed (Fekken, 1999). Recently, the method has been extended with objects that are moving with a prescribed motion (Fekken, 2004).

The simulation of fluid flow in COMFLOW is based on the Navier-Stokes equations for an incompressible, viscous fluid. The equations are discretised using the finite volume method. For the displacement of the free surface the VOF method has been used adapted with a local height function which is essential for a good simulation of the free surface flow. To simulate wave impact in a robust and accurate way, a good choice of the discrete boundary conditions at the free surface turns out to be very important.

In this paper, the numerical method used in COMFLOW is described. Results are shown of the simulation of a steep wave event where the free surface elevation is compared to measurements. Furthermore, the method is validated using results of a simulation with green water on the deck of a moving FPSO due to high regular waves. The amount of water on the deck and pressures at the deck and deck structure are compared with measurements.

## MATHEMATICAL MODEL

Flow of a homogeneous, incompressible, viscous fluid is described by the continuity equation and the Navier-Stokes equations. The continuity equation describes conservation of mass and the Navier-Stokes equations describe conservation of momentum. In conservative form, they are given by

$$\oint_{\partial V} u \cdot n dS = 0, \quad (1)$$

$$\begin{aligned} \int_V \frac{\partial u}{\partial t} dV + \oint_{\partial V} uu^T \cdot n dS = \\ - \frac{1}{\rho} \oint_{\partial V} (pn - \mu \nabla u \cdot n) dS + \int_V F dV. \end{aligned} \quad (2)$$

Here,  $\partial V$  is the boundary of volume  $V$ ,  $u = (u, v, w)$  is the velocity vector in the three coordinate directions,  $n$  is the normal of volume  $V$ ,  $\rho$  denotes the density,  $p$  is the pressure,  $\nabla$  is the gradient operator. Further  $\mu$  denotes the dynamic viscosity and  $F = (F_x, F_y, F_z)$  is an external body force, for example gravity.

In the case that moving rigid bodies are present in the domain  $V$ , the above equations still hold, with the additional condition that the fluid velocity at the boundary of the object is equal to the object velocity.

### Boundary conditions

At the solid walls of the computational domain and at the objects inside the domain, a no-slip boundary condition is used. This condition is described by  $u = 0$  for fixed boundaries, and  $u = u_b$  for moving objects with  $u_b$  the object velocity.

Some of the domain boundaries may let fluid flow in or out of the domain. Especially, when performing wave simulations, an inflow boundary is needed where the incoming wave is prescribed and at the opposite boundary a non-reflecting outflow condition should be used. In our method, the wave on the inflow boundary can be prescribed as a regular linear wave or a regular 5th order Stokes wave. Also a superposition of linear components can be used which results in an irregular wave. At the outflow boundary, a Sommerfeld condition is very appropriate in cases where a regular wave is used. In the case of an irregular wave or a much deformed regular wave (e.g. due to the presence of an object in the flow) a damping zone is added at the end of the domain.

### Free surface

If the position of the free surface is given by  $s(x, t) = 0$ , the displacement of the free surface is described using the following

equation

$$\frac{Ds}{Dt} = \frac{\partial s}{\partial t} + (u \cdot \nabla)s = 0. \quad (3)$$

At the free surface, boundary conditions are necessary for the pressure and the velocities. Continuity of normal and tangential stresses leads to the equations

$$-p + 2\mu \frac{\partial u_n}{\partial n} = -p_0 + 2\gamma H \quad (4)$$

$$\mu \left( \frac{\partial u_n}{\partial t} + \frac{\partial u_t}{\partial n} \right) = 0. \quad (5)$$

Here,  $u_n$  is the normal component of the velocity,  $p_0$  is the atmospheric pressure,  $\gamma$  is the surface tension and  $2H$  denotes the total curvature.

## NUMERICAL MODEL

To solve the Navier-Stokes equations numerically, the computational domain is covered with a fixed Cartesian grid. The variables are staggered, which means that the velocities are defined at cell faces, whereas the pressure is defined in cell centers.

The body geometry is piecewise linear and cuts through the fixed rectangular grid. Volume apertures ( $F^b$ ) and edge apertures ( $A^x$ ,  $A^y$ , and  $A^z$ ) are used to indicate for each cell which part of the cell and cell face respectively is open for fluid and which part is blocked by solid geometry. To track the free surface, the Volume-of-Fluid function  $F^s$  is used, which is 0 if no fluid is present in the cell, 1 if the cell is completely filled with fluid and between 0 and 1 if the cell is partly filled with fluid.

The Navier-Stokes equations are solved in every cell containing fluid. Cell labeling is introduced to distinguish between cells of different characters. First the cells that are completely blocked by geometry are called B(oundary) cells. These cells have volume aperture  $F^b=0$ . Then the cells that are empty, but have the possibility of letting fluid flow in are labeled E(mpty). The adjacent cells, containing fluid, are S(urface) cells. The remaining cells are labeled as F(luid) cells. Note that these cells do not have to be completely filled with fluid. In Figure 1 an example of the labeling is given.

### Discretisation of the continuity equation

The continuity and Navier-Stokes equations are discretised using the finite volume method. The natural form of the equations when using the finite volume method is the conservative

E	E	E	E	E
E	E	S	B	B
S	S	F	F	B
F	F	F	F	F
F	F	F	F	F

Figure 1. Cell labeling: dark grey denotes solid body, light grey is liquid

formulation as given in Eqs. (1) and (2). In this paper, the discretisation is explained in two dimensions. In most situations, this can be extended to three dimensions in a straightforward manner. In Figure 2 a computational cell is shown, which is cut

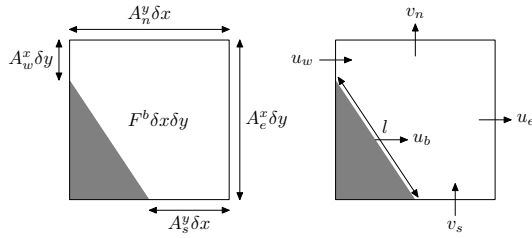


Figure 2. Conservation cell for the continuity equation

by the geometry of a moving body. When applying conservation of mass in this cell, the discretisation results in

$$u_e A_e^x \delta y + v_n A_n^y \delta x - u_w A_w^x \delta y - v_s A_s^y \delta x + u_b (A_e^x - A_w^x) \delta y + v_b (A_n^y - A_s^y) \delta x = 0, \quad (6)$$

where the notation is explained in Figure 2.

### Discretisation of the Navier-Stokes equations

For the discretisation of the Navier-Stokes equations, control volumes are defined containing velocities, which are defined on cell faces. In the case of uncut cells, the control volume of a velocity simply consists of the right half of the cell left of the velocity and the left half of the cell right of the velocity. In case of cut cells a similar procedure to define control volumes has been used, which is explained in detail in (Gerrits, 2001).

The time derivative in the Navier-Stokes equations is discretised in space using the midpoint rule. This results in

tised in space using the midpoint rule. This results in

$$\int_V \frac{\partial u}{\partial t} dV \doteq \frac{\partial u_c}{\partial t} F_c^b \delta x_c \delta y \quad (7)$$

Here,  $u_c$  is the central velocity around which the control volume is placed and  $F_c^b \delta x_c \delta y$  is the volume of the control volume.

The convective term is discretised directly from the boundary integral which is given by

$$\oint_{\partial V} u u \cdot n dS. \quad (8)$$

Note, that this integral contains two different velocities: the scalar velocity  $u$  is advected with the velocity vector  $u$ . This integral is evaluated along all boundaries of the control volume by multiplying the scalar velocity  $u$  with the mass flux through the boundary  $u \cdot n dS$ . Consequently, the discretisation of the convective term results in a matrix that is skew symmetric, which is also a property of the continuous convective operator (Verstappen, 2003).

The diffusive term, which for the Navier-Stokes equation in  $x$ -direction is given by

$$\frac{1}{\rho} \oint_{\partial V} \mu \frac{\partial u}{\partial n} dS, \quad (9)$$

is discretised along all boundaries of the control volume. To ensure stability, the term  $\frac{\partial u}{\partial n}$  is discretised in cut-cells as if the cells are uncut. The error introduced this way is small and has no influence in the convection-dominated simulations. The discretisation results in a symmetric matrix which is negative definite.

The pressure term is discretised as a boundary integral, resulting for the Navier-Stokes equation in  $x$ -direction in

$$\oint_{\partial V} p n_x dS \doteq (p_e - p_w) A_c^x \delta y. \quad (10)$$

Here,  $p_e$  and  $p_w$  are the pressure in the eastern and western cell respectively,  $A_c^x$  is the edge aperture of the cell face where the central velocity is defined. In this way, the discrete gradient operator becomes the transpose of the discrete divergence operator in the continuity equation.

The external force is discretised similar to the time derivative, resulting for the  $x$ -direction in

$$\int_V F_x dV \doteq F_{x_c} F_c^b \delta x_c \delta y. \quad (11)$$

Here,  $F_{xc}$  is the force at the location of the central velocity.

Detailed explanations of the discretisations described in this section are given by (Gerrits, 2001) and (Fekken, 2004).

### Temporal discretisation

The continuity and Navier-Stokes equations are discretised in time using the forward Euler method. This first order method is accurate enough, because the order of the overall accuracy is already determined by the first order accuracy of the free surface displacement algorithm. Using superscript  $n$  for the time level, the temporal discretisation results in

$$Mu_h^{n+1} = 0, \quad (12)$$

$$\Omega \frac{u_h^{n+1} - u_h^n}{\delta t} + C(u_h^n)u_h^n = -\frac{1}{\rho}(M^T p_h^{n+1} - \mu Du_h^n) + F_h^n. \quad (13)$$

The continuity equation is discretised at the new time level to ensure a divergence free velocity field. The spatial discretisation is written in matrix notation where  $M$  is the divergence operator,  $\Omega$  contains cell volumes,  $C$  contains the convection coefficients (which depend on the velocity vector) and  $D$  contains diffusive coefficients.

### Solution method

To solve the system of equations, the equations are rearranged to

$$u_h^{n+1} = \tilde{u}_h^n + \delta t \Omega^{-1} \frac{1}{\rho} M^T p_h^{n+1}, \quad (14)$$

where

$$\tilde{u}_h^n = u_h^n - \delta t \Omega^{-1} (C(u_h^n)u_h^n - \frac{\mu}{\rho} Du_h^n - F_h^n). \quad (15)$$

First, an auxiliary vector field  $\tilde{u}_h^n$  is calculated using Eq. (15). Next, Eq. (14) is substituted in Eq. (12) which results in a Poisson equation for the pressure. From this equation the pressure is solved using the SOR (Successive Over Relaxation) method where the optimal relaxation parameter is determined during the iterations (Botta, 1985). Once the pressure field is known, the new velocity field is calculated from  $\tilde{u}_h^n$  substituting the pressure gradient in Eq. 14.

### Free surface displacement

After the new velocity field has been calculated, the free surface can be displaced. This is done using an adapted version of the Volume-of-Fluid method first introduced by (Hirt, 1981). A piecewise constant reconstruction of the free surface is used, where the free surface is displaced by changing the VOF-value in a cell using calculated fluxes through cell faces.

The original VOF method has two main drawbacks. The first is that flotsam and jetsam can appear, which are small droplets disconnecting from the free surface (Rider, 1998). The other drawback is the gain or loss of water due to rounding of the VOF function. By combining the VOF method with a local height function (Gerrits, 2001), these problems do not appear any more. The local height function is adopted in the following way. For every surface cell, locally a height function is defined, which gives the height of the water in a column of three cells as in Figure 3. The direction in which the function is defined is the direction of the coordinate axis that is most normal to the free surface. Then not the individual fluxes of the three cells are updated, but the height function is updated using fluxes through the boundaries of the column of the three cells (the dashed-lined region in Figure 3). The individual VOF-values of the three cells are then calculated from the height of the water in the column. When using this adopted fluid-displacement algorithm, the method is strictly mass conservative and almost no flotsam and jetsam appear.

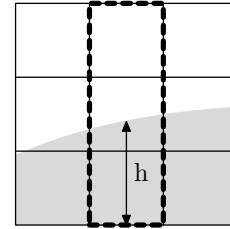


Figure 3. The VOF-function in cells near surface cells are updated using a local height function

### Free surface boundary conditions

At the free surface, boundary conditions are needed for the pressure and the velocities. The pressure in surface cells is calculated as an interpolation or extrapolation from the pressure in an adjacent fluid cell and the boundary condition at the free surface.

The velocities in the neighbourhood of the free surface can be grouped in different classes (see Figure 4). The first class contains the velocities between two F-cells, between two S-cells and between an S- and F- cell. These velocities are determined by solving the momentum equation, so the velocities are called

E	E	E	S
S	S	S	F
S	F	F	F

FF, FS, SS: momentum equation  
SE: extrapolation  
EE: tangential free surface condition

Figure 4. Different characters of velocities near the free surface

momentum velocities. The second class consists of velocities between two E-cells which are sometimes needed to solve the momentum equation. These are determined using the tangential free surface condition. The last class consists of velocities between surface and empty cells (SE-velocities).

The choice for SE-velocities has a large influence on the accuracy and robustness of the method. In the original MAC-method, the SE-velocities are determined by demanding conservation of mass in surface cells (Harlow, 1965). A large disadvantage of this method is, that when cells are cut by the geometry, the resulting SE-velocity calculated from conservation of mass in the S-cell can get very large due to a small edge aperture (see Figure 5). This causes major stability problems when such a configuration stays the same for several consecutive time steps. Therefore, this method has not been adopted in our cut-cell method. Instead, an extrapolation method is proposed, where the SE-velocities are extrapolated from the direction of the main body of the fluid. For accurate wave simulations, a linear extrapolation would be best (see Figure 6), but this causes problems when the velocity field is not smooth. Therefore, a combination of linear and constant extrapolation is used, depending on the smoothness of the local velocity field.

### Stability of the numerical method

In the case of uncut cells with fixed objects, the stability of the equation containing the time integration term and the convective term is given by the CFL-restriction  $\frac{\delta t |u|}{h} \leq 1$ . Here,  $h$  is the size of the uncut cell. When cut cells are present, this criterion is not changed. This result is not directly straightforward when looking at the equation containing the time derivative and the convective term

$$\frac{\partial u}{\partial t} = -\Omega^{-1} C(u, u_b) u \quad (16)$$

where  $u_b$  is the object velocity. The matrix  $\Omega$  is a diagonal matrix containing the volumes of the cells, so these entries can become arbitrary small for cut cells. So the elements in the matrix  $\Omega^{-1}$  can become arbitrary large. But, when estimating the eigenvalues of the convective matrix  $C$  using Gerschgorin circles by being order  $O(\frac{\Omega}{h} u)$  (so the eigenvalues of  $\Omega^{-1} C$  are of order  $O(\frac{u}{h})$ ), it

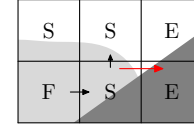


Figure 5. Very large SE-velocity when using mass conservation

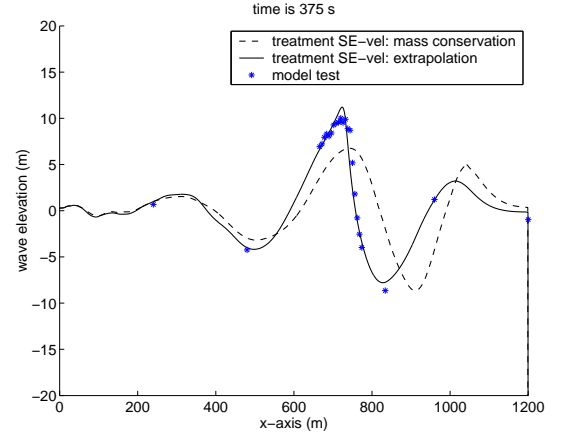


Figure 6. Different methods for SE-velocities in a steep wave simulation

can be concluded that the same stability criterion is needed as for the uncut-cells case (Fekken, 2004).

When moving objects are present, the story becomes somewhat different. Now, the CFL-criterion does not guarantee stability anymore, because the eigenvalues of  $\Omega^{-1} C(u, u_b)$  are of order  $O(\Omega^{-1} h u_b)$  which means that they can become arbitrary large due to the arbitrary large entries of  $\Omega^{-1}$ . To cancel the effect of  $\Omega$  a formulation based on a weighted average of the fluid velocity and the boundary velocity should be applied in the cells cut by the moving object. To avoid smearing of the interface in cases where it is not necessary to stabilise the convective term, the following discretisation is used

$$u^{n+1} = \Omega^{n+1} (\Omega^{n+1} + |\Delta\Omega|)^{-1} (u^n + \delta t (\Omega^{n+1})^{-1} (-C^n u^n)) + (I - \Omega^{n+1} (\Omega^{n+1} + |\Delta\Omega|)^{-1}) u_b^{n+1} \quad (17)$$

where  $\Delta\Omega = \Omega^{n+1} - \Omega^n$  is the difference between  $\Omega$ 's at two different time steps. The factor  $\Omega^{n+1} (\Omega^{n+1} + |\Delta\Omega|)^{-1}$  is chosen because then the stabilising term is only used when the body is moving; note that it equals unity for fixed objects. The maximal stabilisation is required when the object is moving normal to its boundary, whereas no stabilisation is needed when the object is moving tangential to its boundary (see Figure 7). A detailed explanation of the stability of the convective terms is given in (Fekken, 2004).

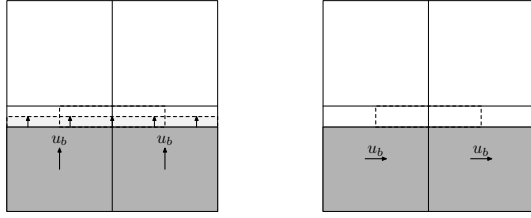


Figure 7. Left: boundary moving normal to itself: maximal stabilisation is required; right: boundary moving tangential to itself: no stabilisation is required

From the diffusive term, also a stability criterion follows with a restriction on the time step. In the case of uncut cells, this criterion is given by  $\delta t \leq \frac{h^2}{2\nu}$ , where  $\nu$  denotes kinematic viscosity. Because the diffusive term is discretised as if all cells were uncut ('staircase' approach), the above criterion is also valid in our model.

## SIMULATION OF STEEP WAVE EVENTS

For the simulation of wave impact at for example the bow of a vessel, an accurate simulation of steep waves is necessary. Therefore, an irregular wave event which has been used for bow impact experiments at the Maritime Research Institute Netherlands (MARIN) is chosen to be simulated with our numerical method. For comparison of the numerical results with the measurements, the wave should be prescribed at the inflow boundary such that the same wave results as in the experiment. Therefore, measurements of a wave probe 720 meter in front of the focusing point of the steep wave event have been used to start up the wave. The time series of the wave height at that wave probe have been analyzed using Fourier transformations. The linear components following from the analysis have been prescribed at the inflow boundary. Although the wave is not linear at that position, the wave prescription turned out to be accurate.

In this paper, results of the simulation of a wave event of a 1/16 steep wave in a sea state steepness for a 100 year return period are shown. The wave is built in such a way, that on beforehand the position and time point where and when the wave is focusing are known. In the top of Figure 8, the time trace of the wave elevation at the focusing point is presented. The numerical prediction of wave height and steepness compare well with the experiment. This can also be seen from the bottom of Figure 8, where the spatial wave elevation has been shown at two different time points. At the time of 428 seconds, the predicted wave is a bit in front of the experiment.

Examining the results, it can be concluded that the current method is able to simulate a steep wave event.

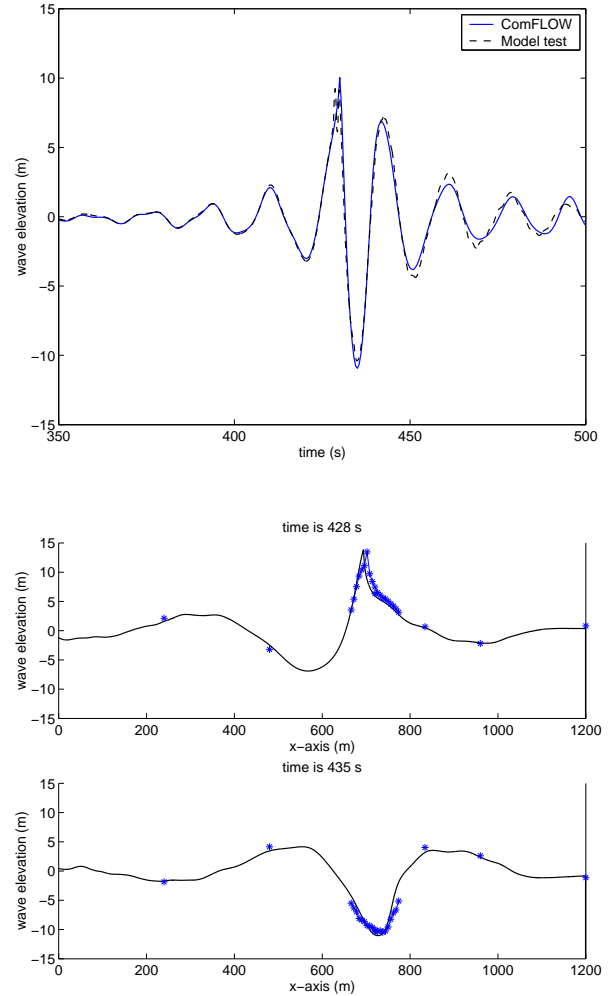


Figure 8. Steep wave event: wave elevation at 720 m behind the inflow boundary (top) and wave elevation at two different time points (bottom)

## GREEN WATER ON THE DECK OF A MOVING FPSO

The ultimate test case for COMFLOW in the current project is the calculation of loads due to green water on the deck of a moving FPSO. For validation, an experiment from the Greenwater JIP performed at MARIN has been used. Measurements were done of the wave in front of the FPSO, relative wave heights in the neighbourhood of the FPSO, water heights and pressures at the deck of the FPSO and the pressure at some places at a deck structure. The FPSO has a total length of 260 meter and is 47 meter wide. The draft is 16.5 meter, the total height of the deck at the fore side of the FPSO is 25.6 meter. There is a bulwark extension of 1.4 meter. At the deck, a box-like structure has been placed at which forces and pressures have been measured. The

bow has a full elliptical shape without flare. The wave that has been chosen has a period of 12.9 seconds and the wave length is 260 meter, equal to the length of the FPSO. The wave amplitude is 6.76 meter. To be sure that the same wave has been used in the experiment and in the simulation, the wave measurement 230 meter in front of the bow of the vessel has been used to initiate the wave at the inflow boundary. The signal from the wave probe has been decomposed in linear components which are prescribed on the inflow boundary. The motion of the ship is prescribed using the measurements of the experiment. The simulation has been performed with only half of the FPSO in a relatively small domain around the bow of the vessel. A grid with 100x60x80 grid points has been used. In Figure 9 some snapshots of the simulation are shown during the first period of the simulation. The large wave is building in front of the vessel after which it starts to flow onto the deck. The water flows off the deck when the ship is straightening.

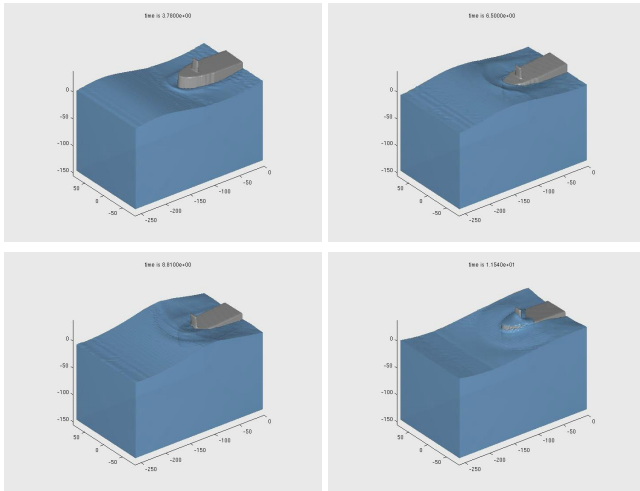


Figure 9. Snapshots of half of an FPSO shipping green water

In Figure 10, the relative wave height in front of the vessel, is shown. In both pictures there is a good agreement, such that it can be concluded that the motion of the vessel relative to the wave motion does not differ much in simulation and experiment. The water height on the deck of the vessel has been compared in Figure 11. When the water has just flowed onto the deck (left figure), the agreement between the experiment and the simulation is reasonable. The moment in time the wave probe gets wet is almost the same. But in the first periods, the water height is somewhat higher in the simulation, whereas the total time the water hits the wave probe is shorter. Closer to the deck structure, in the right of Figure 11, the total amount of water passing the wave probe is much smaller in the simulation. This same behaviour

can be seen from the pressure on the deck and the deck structure. Whereas the pressure at the deck, just behind the fore point of the FPSO agrees reasonably well, the pressure at the deck structure is much lower, indicating that in the simulation only a small amount of fluid reaches the deck structure. The velocity of the water on the deck is quite well predicted by the simulation. The moment in time the water reaches the deck structure is almost exactly the same in experiment and simulation.

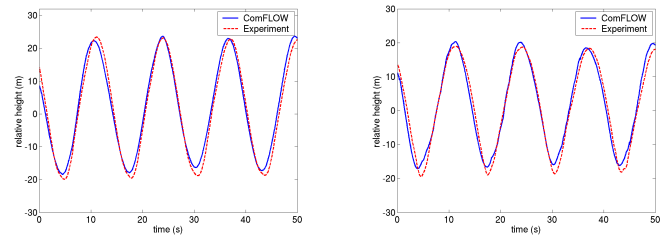


Figure 10. Relative wave height 30 meter (left) and 5 meter (right) in front of the FPSO

There can be several reasons for the differences between simulation and experiment. Firstly, the grid may not be fine enough to simulate the flow on the deck correctly. The vertical size of a cell at the deck is about 0.5 m, meaning that there are at most 10 cells in the water height. Further, there can still be a problem with the phase between the wave and the motion of the

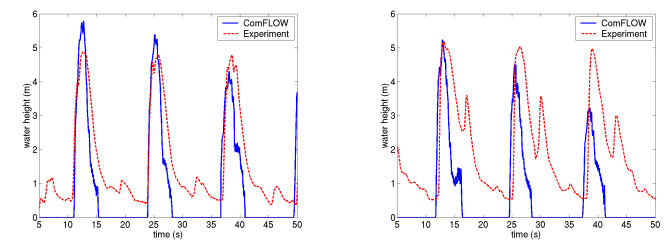


Figure 11. Water height on the deck of the FPSO: at the fore side of the bow (left) and near the deck structure (right)

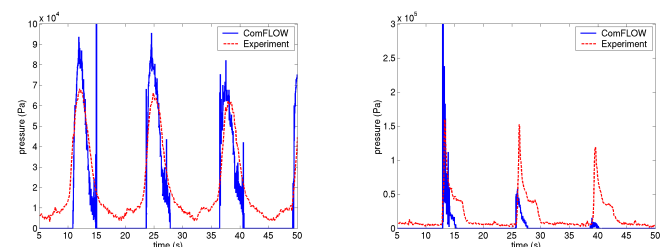


Figure 12. Left: pressure on the deck of the FPSO; right: pressure at the deck structure



vessel which are both prescribed, although this difference seems to be small when looking at the good agreement in Figure 10. To check that, a fully interactive simulation should be performed, where the motion of the vessel is not prescribed, but calculated during the simulation. At the moment, this is not feasible, but in the future this option will be available. One last reason could be the geometry of the ship, which is not exactly the same in the simulation as in the experiment.

## CONCLUSIONS

In this paper, results are shown of the validation of a Navier-Stokes solver with a VOF based free surface displacement. The used cut-cell method on a fixed Cartesian grid is stable even when very small cells appear. The choice of boundary conditions at the free surface turns out to be crucial. The current conditions take care of a very robust method, and give accurate results for wave simulations. The original VOF method for the displacement of the free surface is combined with a local height function, which takes care of full mass conservation.

Results have been shown of the wave elevation in a steep wave event, which are compared with measurements. The wave has been started using linear wave components, following from measurements at a wave probe. The development of the wave in the simulation is very well comparable with the experiment. The method is able to simulate a steep wave. Furthermore, a very demanding simulation of high waves resulting in green water on the deck of a prescribed moving FPSO has been performed. The results show a reasonable agreement with measurements at the start of the simulation. But when the water is flowing onto the deck, the agreement becomes less. Improvement is needed using grid refinement, or by performing a fully coupled simulation of ship motion and fluid flow.

In the further development of the method, already a start has been made with making it a two-phase model. A large advantage is that in two-phase models, no boundary conditions for the velocities are needed at the free surface, which are difficult to determine. In the coming years, the method will also be extended with a coupling to an outer domain where waves are generated using a much cheaper diffraction code. In this way, the COMFLOW domain can be limited to the near surroundings of the places of impact.

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